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A Reliable Method for Predicting the Specific Impulse of Chemical Propellants

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ABSTRACT: The specific impulse (1.) is an important performance parameter that describes energy efficiency of propellant combustion and is intimately related to the rocket engine thrust. In this study, it was possible by using only two variables, i.e., the heat of reaction (Q) and the number of moles of gaseous reaction products per gram of propellant (N_{c}) calculated according to [H_0-CO_] arbitrary decomposition assumption and constants derived from the ISPBKW code to predict the specific impulse of more than 165 compositions belonging to virtually all classes of propellants such as monopropellants, single-base, double-base, triple-base, and cast modified double-base (CMDB) propellants, pseudo-propellants, composite propellants, liquid mono- and bipropellants, and finally hybrid propellants. Further analysis reveals that for C-H-N-O containing propellants, the specific impulse values estimated using the new method should not deviate more than 5% from the output of the ISPBKW thermochemical code.

KEYWORDS: Specific impulse prediction, Solid propellants, Liquid propellants, Hybrid propellants, ISPBKW code.

INTRODUCTION

The first propellant ever created was black powder or gunpowder, which consists of a physical mixture of saltpeter, charcoal and sulfur. For many centuries, this low energy composite mixture served as the sole energetic material for both military and civilian applications. The need for cleaner, more energetic propellants led to the invention of smokeless powder, a homogenous mixture of two well-known explosives substances: nitrocellulose (NC) and nitroglycerine (NG) (Klapötke 2011). For instance, a solid explosive like 2,4,6-Trinitrotoluene (TNT) will detonate when subject to a powerful shock wave but it will only burn or deflagrate when brought into contact with a flame, and hence it is not surprising that most of today's propellants formulations contain large quantities of explosive materials since the thermochemistry of both explosives and propellants is essentially the same (Kubota 2015) but they do differ in their rate of energy release which, to a large extent, depends on the nature and amplitude of the external stimuli that cause them to react in one way or another. Given the relatively long burning time from several seconds to several minutes and coupled with the generation of substantial amounts of hot gaseous products, chemical propellants, whether in solid or liquid state are the principle source of the propulsive force that accelerates rockets, guided missiles and artillery shells. The thrust that a rocket motor develops is directly linked to the specific impulse (I_{sp}) defined as the thrust delivered per unit flow weight of propellants consumed (Bourasseau 1990). Two commonly used units for (I_{o}) are seconds (s) and Ns g⁻¹ (or Ns kg⁻¹). Achieving high (I_{sp}) values is always desirable especially in the case of long range missiles. It can be shown, that almost 45% gain in range can be realized by increasing only 5% the specific impulse of a typical intercontinental ballistic missile having an initial range of 5000 nautical miles (Thompson Jr. 1960).

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More specifically, the rocket combustion chamber temperature (T_c) and the average molecular weight (\overline{M}) of the exhaust gas are the primary dominant factors determining the specific impulse (Kinney 1960). Thus, the relationship relating (I_{sp}) to (T_c) and (\overline{M}) is shown by:

$$I_{sp} \propto \sqrt{T_c/\overline{M}}$$
 (1)

As Eq. 1 states, this highest (I_{sp}) value can be reached by finding a propellant formulation capable of generating the highest (T_c) and the lowest possible (M). However, during rocket operation, the combustion chamber walls may be weakened due to the large heat transfer from the burning propellant, which can ultimately lead to a catastrophic structural failure; therefore combustion temperature should be kept at an acceptable level without sacrificing overall performance. Another problem facing propellant formulators is the difficulty encountered in the experimental evaluation of the specific impulse that requires hundreds of kilograms of potentially dangerous and explosives energetic materials (Bhat *et al.* 1988; Lempert *et al.* 2011). Consequently, researchers rely heavily on thermochemical code such as NASA CEA (Gordon and McBride 1996) or TERRA code (Trusov 2002) to accurately compute propellant performance at a determined pressure ratio defined as $(P_c; P_a)$ where (P_c) and (P_a) are the combustion chamber pressure and the ambient pressure at the nozzle exit, respectively. Similarly to thermochemical codes, relationships derived from empirical data present a viable alternative to compute the performance of explosives and propellants. Recent studies show that condensed explosive detonation velocity (Keshavarz 2012), pressure (Keshavarz *et al.* 2014), temperature (Keshavarz and Nazari 2006) and other performance parameters (Frem 2017), as well as the specific impulse of monopropellants (Frem 2016), can be precisely calculated using only few experimental data (e.g. crystal density, heat of formation, etc.) and no more than a hand-held calculator. Accordingly, the intent of the next section is to present a detailed derivation of a new and simple method for predicting the specific impulse of C-H-N-O chemical propellants that do not contain any metal additives such as aluminum.

RESULT AND DISCUSSION

NEW RELATIONSHIP FOR THE ESTIMATION OF THE SPECIFIC IMPULSE (Isp)

The driving force behind the current study was the work of Kamlet & Jacobs (K-J) published in 1968 (Kamlet and Jacobs 1968), where the authors have showed that the detonation velocity (D) and pressure (P) for C-H-N-O containing explosives can be predicted following Eqs. 2 and 3:

$$D(mm\,\mu s^{-1}) = A\Phi^{0.5}(1+B\rho_0) \tag{2}$$

$$P(kbar) = K\rho_0^2 \Phi \tag{3}$$

where: ρ_0 (g·cm⁻³) is the explosive initial density; *A*, *B*, *K* are constants and equal to 1.01, 1.30, and 15.58, respectively, while; (N_g) is the number of moles of gaseous detonation products per gram of explosive; (M_g) is the average molecular weight of these gases; and (*Q*) is the heat of detonation in (cal·g⁻¹). The (K-J) method presumes that for C-H-N-O explosives at an initial $\rho_0 = 1.7 - 1.9$ g·cm⁻³, the major decomposition products are water (H₂O), carbon dioxide (CO₂) and nitrogen (N₂), and often termed the [H₂O-CO₂] arbitrary decomposition assumption. Despite its simplicity, the detonation velocity and pressure calculated using the [H₂O-CO₂] arbitrary are in good agreement with the value obtained using complex thermochemical codes. The (Φ) parameter was later used to obtain the Gurney velocity ($\sqrt{2E_G}$) (Hardesty and Kennedy 1977; Kamlet and Finger 1979), an important performance parameter that represents the ability of a given explosive to push and accelerate a surrounding metal shell. Given the fact that explosives and propellants possess comparable energy content and, in many cases similar chemical compositions, it was felt that the [H₂O-CO₂] arbitrary could, in principle, be used to estimate the specific impulse. To test this hypothesis, a thorough study was made in order to uncover the potential influence of (N_g), (M_g), and (Q) on specific impulse. The results show, that only (N_g) and (Q) were significant in obtaining a relationship capable of accurately predicting propellant (I_{go}) (Eq. 4):

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$$I_{sp}^{2} = X_{1} + C_{1}(N_{g}) + C_{2}(Q)$$
⁽⁴⁾

where the intercept X_1 and the coefficient $C_1 - C_2$ were derived using a multiple linear regression analysis (MLRA) and the computed (I_{sp}) values for thirty-seven C-H-N-O monopropellants shown in Table 1 (Eq. 5):

$$I_{sp}(Ns \ g^{-1}) = \sqrt{-4.459 + 121.81 \left(N_g\right) + 4.697 \left(Q\right)}$$
(5)

where (*Q*) and (N_g), now termed the heat of reaction in (kcal g⁻¹) and the number of moles of gaseous reaction products per gram of propellant, respectively, were calculated according to Eqs. 6 and 7:

$$Q = \frac{28.9b + 47(d - b/2) + \Delta H_f^{o}}{M_w}$$
(6)
$$N_g = \frac{2c + 2d + b}{48a + 4b + 56c + 64d}$$
(7)

where: *a*, *b*, *c* and *d* are the number of carbon (C), hydrogen (H), nitrogen (N) and oxygen (O) atoms in the propellant composition, $(\Delta H_{f}^{\circ} \text{ kcal mol}^{-1})$ represents the condensed phase heat of formation (HOF), and M_{w} is the composition's molecular weight. The calculated specific impulse of the training set was obtained using the ISPBKW thermochemical code (Mader 2008) at a predetermined chamber and nozzle exit pressure of 68.9 and 1 bar ($P_c: P_a = 68.9:1$), respectively. The coefficient of determination (R^2) of the regression equation is equal to 0.948. Relevant statistical results (*t*-stat, *P*-values, regression coefficients $C_1 - C_2$, etc.) obtained from the (MLRA) are summarized in Table 2. The *P*-values < 0.05 and the *t*-values clearly indicate that the suggested independent variables are significant to estimate specific impulse. Moreover, the very small significance *F* value (1.45810⁻²²) confirms the validity of the regression output.

It can be seen from Table 1 that there is a good agreement between the specific impulses calculated using the ISPBKW code and the values obtained by applying Eq. 5 and in all of the studied cases the deviation did not exceed $\pm 3 - 4\%$.

The intention of the next sections is to evaluate the predictive ability of the obtained model by using a test set comprising not only solid single component monopropellants, but also multicomponent solid, liquid, and hybrid propellants.

SINGLE MOLECULE MONOPROPELLANTS

The monopropellants shown in Fig. 1 were carefully chosen so as to cover the most important class of energetic molecules such as nitroaromatics, aliphatic nitrate esters and salts of high-nitrogen content heterocycles. Moreover, the specific impulses for the twenty studied structures were predicted using both Eqs. 5 and 8:

$$I_{sp}(Ns \ g^{-1}) = 2.4205 - 0.0740a - 0.0036b + 0.0237c + 0.0400d - 0.1001n_{NH_x} + 0.1466 \ (n_{Ar} - 1)$$
(8)

where: *a*, *b*, *c* and *d* are the number of carbon (C), hydrogen (H), nitrogen (N) and oxygen (O) atoms while is the number of -NH and $-NH_2$ groups, and (n_{Ar}) is the number of aromatic rings that might be present in the propellant compositions (Keshavarz 2008). Since both Eqs. 5 and 8 were derived with the help of the ISPBKW code, it will be useful to compare the predictive power of each of them with the code output. The results reported in Table 3 show that the specific impulses calculated using Eq. 5 are in good agreement (3 – 4% deviation) with the actual values obtained from the ISPBKW code. On the other hand, the application of Eq. 8 can, in certain instances, result in a large deviation (> 7%) in the calculated (I_{sp}) such as in the cases of structures showed in Figs. 1b, 1c, 1f, 1l, 1m, and 1q to 1t.

	monopropella	ant compositions. Pei	rcentage deviations ii	n parentheses.	
Compositions	Δ H ⁰ _f (kcal mol⁻¹)ª	N_{g}	Q∕ (kcal g⁻¹)	<i>I_{sp}∕</i> (Ns g⁻¹)º	<i>I_{sp}</i> (Eq. 5)∕(Ns g⁻¹) ^d
PETN	-128.7	0.0316	1.514	2.58	2.55 (-1.23%)
TNT	-16.0	0.0253	1.291	2.11	2.17 (2.62%)
HMX	17.93	0.0338	1.477	2.62	2.57 (-1.86%)
RDX	14.71	0.0338	1.482	2.62	2.57 (-1.81%)
Tetryl	4.67	0.0270	1.420	2.35	2.35 (0)
NM	-27.0	0.0369	1.364	2.46	2.54 (3.23%)
HNS	18.7	0.0233	1.367	2.19	2.19 (0%)
Comp-B	1.28	0.0308	1.410	2.42	2.43 (0.52%)
PBX-9404	0.08	0.0337	1.414	2.55	2.51 (-1.90%)
PBX-9011	-4.05	0.0333	1.358	2.43	2.44 (0.59%)
LX-14	1.5	0.0336	1.423	2.54	2.51 (-1.04%)
Pentolite (50/50)	-23.9	0.0285	1.402	2.37	2.37 (0)
HNAB	67.9	0.0243	1.445	2.32	2.30 (-0.92%)
NG	-88.6	0.0319	1.591	2.53	2.63 (3.67%)
NQ	-22.1	0.0385	0.898	2.11	2.11 (0)
Octol (75/25)	2.78	0.0317	1.431	2.50	2.47 (-0.95%)
TATB	-36.85	0.0291	1.075	2.01	2.03 (1.26%)
PA	-51.3	0.0251	1.283	2.18	2.15 (-1.47%)
Cyclotol (60/40)	1.15	0.0304	1.406	2.42	2.42 (0)
DEGDN	-99.4 ^b	0.0332	1.392	2.42	2.47 (2.20%)
PBX-9007	7.13	0.0324	1.392	2.39	2.46 (2.83%)
PBX-9501	2.28	0.0336	1.442	2.56	2.53 (-1.29%)
DIPAM	-6.80	0.0253	1.298	2.16	2.17 (0.49%)
BTNEU	-76.91 ^b	0.0311	1.467	2.52	2.49 (-0.89%)
BTTN	-97.04 ^b	0.0322	1.509	2.59	2.56 (-1.18%)
FOX-7	-32.00 ^b	0.0338	1.199	2.38	2.30 (-3.40%)
DDNP	46.39 ^b	0.0238	1.391	2.27	2.23 (-1.93%)
DNDMOxm	-73.00 ^b	0.0316	1.171	2.22	2.21 (-0.26%)
DNOC	-47.80 ^b	0.0253	1.109	1.93	1.96 (1.34%)
DNPH	11.95 ^b	0.0278	1.173	2.07	2.11 (1.87%)
DINA	-65.88 ^b	0.0333	1.472	2.56	2.55 (-0.44%)
DIPEHN	-233.79 ^b	0.0315	1.422	2.49	2.46 (-1.03%)
ETN	-114.76 ^b	0.0325	1.365	2.34	2.43 (4.02%)
EDDN	-156.18 ^b	0.0403	0.966	2.20	2.23 (1.49%)
EDNA	-24.81 ^b	0.0367	1.303	2.46	2.48 (0.69%)
GUNI	-92.52 ^b	0.0410	0.662	1.90	1.91 (0.31%)
FOX-12	-85.09 ^b	0.0371	0.898	2.15	2.07 (-3.95%)

 Table 1. Comparison between the specific impulse values calculated using the ISPBKW code and Eq. 5 for different monopropellant compositions. Percentage deviations in parentheses.

"Heat of formations (HOFs): (Dobratz and Crawford 1985) otherwise stated; "(Meyer *et al.* 2007); "Equilibrium specific impulses were calculated using the ISPBKW thermochemical code (Mader 2008); "To convert to the more conventional units of seconds, divide by 0.00981 Ng⁻¹.

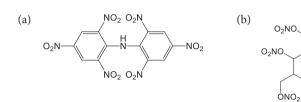


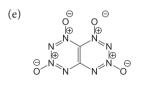
Table 2. Coefficients, standard errors, t-statistics, statistical significance (P-values), the lower and upper boundsof the 95% confidence intervals of Eq. 5 obtained by multiple regression analysis ($R^2_{adjusted}$ = 0.945).

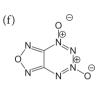
	Coefficients	Standard Error	t-Stat	P-value	Lower 95%	Upper 95%
Intercept	-4.459	0.437	-10.193	7.13 10-12	-5.348	-3.570
N_{g}	121.81	8.62	14.135	8.51 10-16	104.29	139.32
Q	4.697	0.193	24.328	4.36 10-23	4.305	5.090

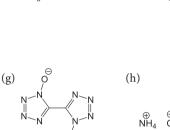
ONO₂

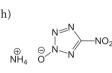
ONO₂







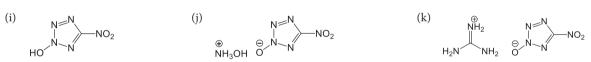


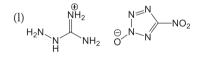


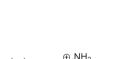
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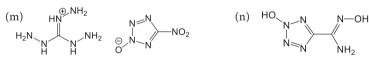
⊕ (NH₃OH)₂

(c)









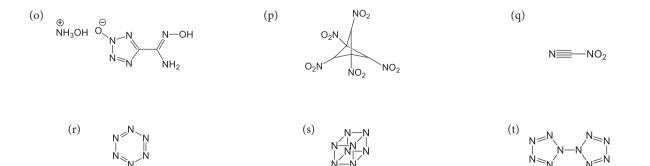


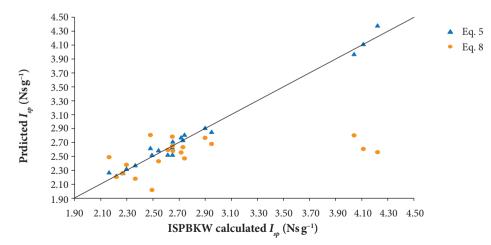
Figure 1. Structural formulas of different C-H-N-O, CNO and N_x (x = 6,8,10) monopropellants.

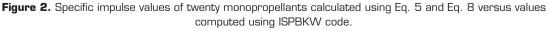
Compositions	∆ <i>H⁰_f</i> (kcal mol⁻¹)	N _g	<i>Q∕</i> (kcal g⁻¹)	<i>I_{sp}∕</i> (Ns g⁻¹) ^j	<i>I_{sp}</i> (Eq. 5) (Ns g⁻¹)	<i>I_{sp}</i> (Eq. 8) (Ns g⁻¹)
1a	9.88ª	0.0245	1.368	2.22	2.22 (0)	2.21 (-0.55%)
1b	-161.53ª	0.0310	1.609	2.48	2.62 (5.71%)	2.81(13.30%)
1c	-84.31ª	0.0426	0.947	2.16	2.27 (5.13%)	2.49 (15.22%)
1d	144.5 ^b	0.0238	1.692	2.65	2.53 (-4.63%)	2.65 (0)
1e	207.53°	0.0300	1.978	2.90	2.91 (0.48%)	2.77 (-4.49%)
1f	161.02 ^c	0.0288	1.936	2.95	2.85 (-3.24%)	2.68 (-9.11%)
1g	106.74^{d}	0.0381	1.432	2.65	2.63 (-0.70%)	2.79 (5.27%)
1h	36.33 ^e	0.0372	1.344	2.61	2.53 (-3.36%)	2.59 (-0.75%)
1i	73.76 ^e	0.0324	1.681	2.65	2.72 (2.52%)	2.58 (-2.63%)
1j	52.27 ^e	0.0366	1.597	2.73	2.74 (0.30%)	2.63 (-3.51%)
1k	32.67 ^e	0.0368	1.085	2.27	2.26 (-0.29%)	2.26 (-0.43%)
11	61.28 ^e	0.0378	1.171	2.37	2.38 (0.48%)	2.18 (-7.81%)
1m	112.69 ^e	0.0394	1.286	2.49	2.53 (1.34%)	2.02 (-18.93%)
1n	56.96 ^f	0.0347	1.198	2.30	2.32 (1.20%)	2.38 (3.67%)
10	67.38 ^f	0.0381	1.391	2.54	2.59 (1.97%)	2.43 (-4.28%)
1p	58.66 ^g	0.0282	1.860	2.72	2.78 (2.24%)	2.56 (-5.78%)
1q	43.90^{h}	0.0278	1.915	2.74	2.81 (2.64%)	2.47 (-9.78%)
1r	345.6 ⁱ	0.0357	4.114	4.22	4.38 (3.87%)	2.56 (-39.28%)
1s	406.7 ⁱ	0.0357	3.631	4.11	4.12 (0.11%)	2.61 (-36.53%)
1t	473.4 ⁱ	0.0357	3.381	4.04	3.97 (-1.73%)	2.80 (-30.62%)
RMSD (Ns g ⁻¹)*					0.08	0.602

Table 3. Comparison between the specific impulse values calculated using Eqs. 5 and 8 to ISPBKW code results for different monopropellant compositions. Percentage deviations in parentheses.

"[Meyer *et al.* 2007]; "[Dobratz and Crawford 1985]; "(Christe *et al.* 2015); "(Fischer *et al.* 2012); "(Gibel *et al.* 2010); "(Klapötke *et al.* 2015); "(Ghule *et al.* 2011); "(Rahm *et al.* 2014); "(Lempert *et al.* 2009); Equilibrium specific impulses were calculated using the ISPBKW thermochemical code (Mader 2008). *RMSD = Root-Mean-Square Deviation.

A graphical plot of the predicted (I_{sr}) using Eq. 5 and Eq. 8 versus ISPBKW code results is depicted in Fig. 2.





It can be shown that the data points obtained using the Keshavarz's method are more scattered around the diagonal line bisecting the graph (i.e. the line of perfect agreement between predicted and code results) compared to the ones obtained using the new method. Obviously, the major advantage of using Eq. 5 over Eq. 8 is the capability of the first to accurately predict the specific impulse of the yet hypothetical homoleptic polynitrogen compounds possessing the general formula $N_x(x = 6, 8, 10, \text{etc.})$.

SINGLE, DOUBLE, AND TRIPLE-BASE PROPELLANTS

Typical single-base (SB), double-base (DB), composite modified double-base (CMDB) and triple-base (TB) propellant formulations are listed in Table 5. Single-base propellants contain nitrocellulose, which has been gelatinized in acetone or in alcohol-ether solvent mixture and to which has been added various additives in order to improve the quality of the propellant powder. Likewise, double-base (DB) propellants are mixtures of nitrocellulose and nitroglycerine along with other additives, such as plasticizers, stabilizers and burn rate controllers, all of which alter the mechanical and thermal properties of the composition. The incorporation of solid oxidizers (e.g. ammonium perchlorate, ammonium dinitramide, etc.) and in some cases metallic fuel (e.g. aluminum) into the (DB) formulation, results in the formation of composite modified double-base (CMDB) propellants characterized by high specific impulse figures (Agrawal 2010).

Compositions	Atomic compositions	∆ <i>H</i> ° _ŕ (kcal mol⁻¹)
NG	C ₃ H ₅ N ₃ O ₉	-88.6ª
NC (12% N)	$C_6 H_{7.74} N_{2.26} O_{9.52}$	-173.7ª
NC (13.35% N)	$C_6H_{7,29}N_{2,71}O_{10,41}$	-163.0^{a}
NQ	$CH_4N_4O_2$	-22.1ª
RDX	$C_3H_6N_6O_6$	+14.71ª
BDNPA-F (50/50 BDNPA/BDNPF)	$C_{2.347}H_{4.068}N_{1.254}O_{3.134}$	-46.39^{a}
DEP	$C_{12}H_{14}O_{4}$	-179.99 ^b
2-NDPA	$C_{12}H_{10}N_2O_2$	18.40 ^b
AP	$\rm NH_4ClO_4$	-70.58^{a}
ADN	$H_4N_4O_4$	-35.99°
HNF	CH ₅ N ₅ O ₆	-17.21°
TAGAZ	$C_4 H_8 N_{22}$	257.0 ^d
Carbamite	$C_{17}H_{20}N_2O$	-105.06 ^e
DNC 90/7/3 NC(12% N)/NG/Carbamite	$C_{2.329}H_{3.017}N_{0.886}O_{3.535}$	-62.27
CL 78/20/2 NG/DEP/2-NDPA	$C_{2.22}H_{3.07}N_{1.05}O_{3.47}$	-46.48

Table 4. Atomic compositions and heat of formations of different ingredients used in triple-base and CMDB propellant compositions.

«(Dobratz and Crawford 1985); » (NIST 2017); « (Gadiot *et al.* 1993); « (Sivabalan *et al.* 2004);« (Meyer *et al.* 2007).

On the other hand, standard triple-base (TB) propellants contain nitroguanidine (picrite), which has been added to the (NC-NG) matrix in order to reduce muzzle flash and gun barrel erosion (U.S. Army Material Command 1965). The condensed heats of formation and atomic compositions of (CMDB) and (TB) propellants (except M15, M17 and T34) were calculated from their individual ingredients shown in Table 4. The estimated specific impulses using Eq. 5 were in close agreement with thermochemical code results. Upon combustion, ammonium perchlorate containing compositions produces hydrogen chloride which is not taken into account in calculating the value of (N_g) and (Q), which explains the relatively high deviation of about ~4% in the predicted specific impulse for the CMBD formulations containing 29.5% ammonium perchlorate. It should be noted that many of the investigated (SB), (DB) and (TB) formulations contain small amount of mineral additives (e.g. KNO_3 , K_2SO_4) used as flash reducers; however in this study, these salts were excluded in computing the (I_{ab}) values.



Table 5. Comparison between the specific impulse values calculated using the ISPBKW code and Eq. 5 for single-base, double-base, triple-base and CMDB propellant compositions. Percentage deviations in parentheses.

uuunie-nase, unpie-nase anu uvin	D highenanic compos		ercentaye uevia	uons in parenu	leses.
Single-base propellants	Δ <i>H</i> ° _f (kcal mol⁻¹)ª	N _g	<i>Q∕</i> (kcal g⁻¹)	/ _{<i>sp</i>} ∕ (Ns g ⁻¹) ^f	/ _{<i>₅p</i>} (Eq. 5) (Ns g⁻¹)
M1	-53.80	0.0291	1.213	2.12	2.19 (3.07%)
M1A1	-57.40	0.0292	1.179	2.07	2.15 (3.80%)
M6	-53.80	0.0292	1.228	2.16	2.21 (2.00%)
M10	-59.30	0.0298	1.256	2.27	2.25 (-1.02%)
M12	-56.80	0.0296	1.245	2.23	2.23 (0)
M14	-54.10	0.0292	1.242	2.20	2.22 (1.06%)
IMR	-56.80	0.0296	1.247	2.24	2.24 (0)
Double-base propellants	∆ <i>H</i> ° _f (kcal mol⁻¹)ª	N _g	<i>Q∕</i> (kcal g⁻¹)	<i>l_{sp}</i> ∕ (Ns g ⁻¹) ^f	/ _{sp} (Eq. 5) (Ns g⁻¹)
M2	-55.90	0.0304	1.319	2.37	2.33 (-1.75%)
M5	-56.80	0.0303	1.304	2.35	2.31 (-1.55%)
M7	-48.30	0.0302	1.387	2.45	2.39 (-2.27%)
M8	-47.50	0.0305	1.410	2.48	2.42 (-2.17%)
M9	-47.70	0.0305	1.422	2.50	2.44 (-2.47%)
M18	-55.70	0.0295	1.232	2.17	2.22 (2.11%)
M26	-50.40	0.0300	1.307	2.31	2.31 (0)
T25	-52.10	0.0299	1.295	2.30	2.29 (-0.47%)
Triple-base propellants	ΔH ° (kcal mol-1)ª	N _g	<i>Q∕</i> (kcal g⁻¹)	<i>l_{sp}</i> ∕ (Ns g ⁻¹) ^f	/ _{sp} (Eq. 5) (Ns g⁻¹)
M15	-30.20	0.0346	1.094	2.19	2.21 (0.97%)
M17	-31.90	0.0349	1.137	2.30	2.26 (-1.65%)
T34	-33.10	0.0347	1.088	2.20	2.21 (0.50%)
28/22.5/1.5/48 NC (12% N)/NG/Carbamite/Picrite^ b	-37.56	0.0343	1.131	2.28	2.24 (-1.63%)
28/22.5/1.5/48 NC (13.35% N)/NG/Carbamite/Picrite^ $$	-35.20	0.0343	1.157	2.32	2.27 (-2.09%)
20.8/20.6/3.6/55 NC (13.35% N)/NG/Carbamite/Picrite^b $$	-32.00	0.0347	1.107	2.25	2.23 (-0.81%)
28/22.5/1.5/38/10 NC (12% N)/NG/Carbamite/ Picrite/RDX ^c	-34.77	0.0339	1.189	2.33	2.29 (-1.77%)
28/22.5/1.5/33/15 NC (12% N)/NG/Carbamite/ Picrite/RDX ^c	-33.38	0.0336	1.219	2.36	2.32 (-1.75%)
28/22.5/1.5/28/20 NC (12% N)/NG/Carbamite/ Picrite/RDX ^c	-31.98	0.0334	1.248	2.38	2.34 (-1.86%)
CMDB propellants	ΔH_{f}° (kcal mol ⁻¹) ^a	N _g	<i>Q∕</i> (kcal g⁻¹)	<i>l_{sp}</i> ∕ (Ns g ⁻¹) ^f	/ _{sp} (Eq. 5) (Ns g⁻¹)
29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/APd	-54.96	0.0329	1.251	2.42	2.33 (-3.95%)
29.5/32/2/1/29.5/6 DNC/NG/DEP/2-NDPA/AP/ BDNPA-F ^d	-52.88	0.0334	1.302	2.49	2.39 (-4.01%)
29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/RDX ^d	-35.30	0.0311	1.339	2.38	2.37 (-0.50%)
29.5/32/2/1/29.5/6 DNC/NG/DEP/2-NDPA/RDX/ BDNPA-F ^d	-33.23	0.0316	1.390	2.47	2.43 (-1.58%)
29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/ADN	-45.82	0.0331	1.314	2.45	2.40 (-2.10%)
29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/HNF	-40.03	0.0320	1.372	2.47	2.43 (-1.65%)
30/40/30 DNC/CL/TAGAZ ^e	-16.68	0.0334	1.177	2.18	2.27 (3.96%)

*Chemical compositions and heat of formations (HOFs): (Baer and Bryson 1961) otherwise stated; Other chemical compositions: *(Sanghavi et al. 2003); *(Sanghavi et al. 2003); *(Soughavi et al. 2004); *(Soughavi et al. 2004

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PSEUDO-PROPELLANTS

Pseudo-propellants are homogenous mixtures formed by physically mixing two or more ingredients possessing particle sizes on the order of 10 µm or less (Beckstead 2006). Numerical and experimental studies have been performed in order to study the combustion behavior and flame structure of pseudo-propellants especially nitramine/energetic binder binary systems (Kim et al. 2002; Lee et al. 1999). The use of energetic binders in propellant formulations has a distinctive advantage over traditional inert binders (e.g. HTPB) because they offer substantial additional energy during burning, which ultimately increases the overall specific impulse (Talawar et al. 2009). Some of the most studied nitramine-based pseudo-propellants are listed in Table 6 along with the calculated and estimated (I_{sp}) values, where one can clearly see that there is a very good agreement between the specific impulse values predicted using Eq. 5 and thermochemical code output.

Pseudo-propellant compositions	Δ <i>H</i> ° _{<i>f</i>} (kcal mol⁻¹)ª	N_{g}	<i>Q</i> ∕(kcal g⁻¹)	<i>I_{sp}∕</i> (Ns g⁻¹)⁵	<i>I_{sp}</i> (Eq. 5) (Ns g⁻¹)
80/20 RDX/GAP	10.96	0.0336	1.392	2.46	2.48 (1.03%)
71/9/20 RDX/GAP/BTTN	-0.96	0.0334	1.445	2.55	2.53 (-0.87%)
70/30 HMX/GAP	12.73	0.0335	1.342	2.35	2.43 (3.61%)
80/20 RDX/BAMO	17.26	0.0335	1.408	2.49	2.50 (0.16%)
70/30 HMX/BAMO	22.17	0.0334	1.367	2.41	2.46 (1.91%)
70/30 CL-20/GAP	23.89	0.0314	1.416	2.44	2.45 (0.48%)
80/20 CL-20/BAMO	29.56	0.0312	1.488	2.58	2.51 (-2.47%)

Table 6. Comparison between the specific impulse values calculated using the ISPBKW code and Eq. 5 for nitramine-based pseudo-propellant compositions. Percentage deviations in parentheses.

^a Heat of formation (HOF) and chemical composition of GAP and BAMO: [Gadiot et al. 1993); (HOF) of BTTN and CL-20: (NIST 2017) and (Meyer et al. 2007), respectively; ^bEquilibrium specific impulses were calculated using the ISPBKW thermochemical code (Mader 2008).

COMPOSITE PROPELLANTS

Ammonium perchlorate (AP)-based composite propellants (CPs) are by far the most important class of solid rocket propellants. Typical compositions are heterogeneous mixtures of an oxidizer mainly AP (60 - 80%) dispersed in a polymeric binder (e.g. HTPB, 10 - 15%) to which a metallic fuel such as aluminum (15 - 20%) may be added (Jain et al. 2009). Moreover, AP-based (CPs) offers high performance and excellent mechanical properties (Davenas 1993); however, they have some drawbacks, including the generation of large amounts of pollutants like toxic hydrogen chloride gas, which contributes to the depletion of the ozone layer (Lempert et al. 2006). Furthermore, the interaction of hydrogen chloride with the ambient atmosphere stimulates moisture condensation resulting in the formation of white secondary smoke, thereby making the firing position highly vulnerable to hostile action (Chaturvedi and Dave 2015). The need for powerful propellants with low environmental impact led to the development of chlorine-free oxidizers such as ammonium dinitramide (ADN) and hydrazinium nitroformate (HNF) which, in combination with suitable binders, can yield highly performant (CPs). The specific impulses for a number of (CP) formulations based on (ADN), (HNF) ammonium nitrate (AN) and high-enthalpy C-N-O organic oxidizers (see Fig. 3) have been calculated and are shown in Table 7.

The good agreement (\pm 3 – 4% deviation) seen between ISPBKW code and Eq. 5 calculations indicates that the new model is capable of accurately predict the specific impulse of composite propellants having diverse chemical compositions and a wide range of performance capabilities.

LIQUID MONOPROPELLANTS AND BIPROPELLANTS

From an engineering point of view, a solid rocket motor (SRM) has far fewer components than a liquid rocket engine (LRE). While a (SRM) is basically a propellant charge (grain) fitted inside a metallic case to which is attached a supersonic exhaust nozzle, a (LRE) consists of a myriad of parts including thrust chambers, propellant tanks connected to a piping network, power sources, **Table 7.** Comparison between the specific impulse values calculated using the ISPBKW code and Eq. 5 for ADN, AN, HNF, and organic oxidizer-based composite propellant compositions. Percentage deviations in parentheses.

			l ci centage acvi		
ADN-based compositions	Δ <i>H</i> ° _f (kcal mol⁻¹)	Ng	@∕(kcal g⁻¹)	/ _{<i>sp</i>} ∕ (Ns g⁻¹) ^f	/ _{sp} (Eq. 5) (Ns g⁻¹)
80/20 ADN/GAP ^a	-17.55	0.0388	1.326	2.60	2.55 (-1.99%)
75/25 ADN/GAP ^a	-14.69	0.0384	1.307	2.57	2.52 (-1.89%)
70/30 ADN/GAP ^a	-11.82	0.0381	1.289	2.53	2.50 (-1.29%)
65/35 ADN/GAP ^a	-8.96	0.0377	1.270	2.48	2.47 (-0.37%)
60/40 ADN/GAP ^a	-6.09	0.0373	1.252	2.42	2.44 (0.77%)
50/50 ADN/GAP ^a	-0.36	0.0366	1.215	2.29	2.39 (4.21%)
74/26 ADN/AB ^b	-26.17	0.0384	1.397	2.47	2.60 (5.53%)
85/15 ADN/PMVT ^b	-20.16	0.0390	1.279	2.57	2.51 (-2.36%)
80/20 ADN/PVMDO ^b	-23.21	0.0391	1.367	2.62	2.59 (-0.97%)
AN-based compositions	Δ <i>H</i> ° _{<i>f</i>} (kcal mol⁻¹)	N _g	@∕(kcal g⁻¹)	/ _{<i>sp</i>} ∕ (Ns g ⁻¹) ^f	<i>l_{sp}</i> (Eq. 5) (Ns g⁻¹)
75/25 AN/AB ^b	-86.28	0.0410	1.054	2.29	2.34 (2.44%)
75/25 AN/PMVT ^b	-88.16	0.0420	0.889	2.24	2.20 (-2.10%)
85/15 AN/PVMDO ^b	-92.66	0.0423	0.986	2.34	2.31 (-1.47%)
60/20/20 AN/GAP/TMETN ^c	-112.41	0.0393	0.614	1.85	1.79 (-3.27%)
70/15/15 AN/GAP/TMETN ^c	-111.56	0.0404	0.696	2.01	1.93 (-4.16%)
60/15/15/10 AN/GAP/TMETN/NC(12%N) ^c	-107.24	0.0390	0.721	1.99	1.92 (-3.70%)
40/15/15/30 AN/GAP/TMETN/NC(12%N) ^c	-98.61	0.0362	0.772	1.94	1.89 (-2.43%)
40/15/15/30 AN/GAP/TMETN/HMX ^c	-77.04	0.0374	0.856	2.08	2.03 (-2.46%)
HNF-based compositions	Δ <i>H</i> ° _f (kcal mol⁻¹)	Ng	@∕(kcal g⁻¹)	/ _{<i>sp</i>} ∕ (Ns g⁻¹) ^f	/ _{sp} (Eq. 5) (Ns g⁻¹)
80/20 HNF/GAP ^d	-1.86	0.0361	1.481	2.66	2.63 (-1.40%)
80/20 HNF/PGN ^d	-18.95	0.0358	1.522	2.65	2.66 (0.22%)
80/20 HNF/PLN ^d	-19.55	0.0372	1.539	2.70	2.70 (0)
80/20 HNF/BAMO ^d	4.44	0.0360	1.498	2.68	2.64 (-1.63%)
80/20 HNF/HTPB	-10.29	0.0351	1.383	2.40	2.51 (4.57%)
Organic oxidizer-based compositions	ΔH_{f}° (kcal mol ⁻¹)	Ng	Q∕(kcal g⁻¹)	/ _{<i>sp</i>} ∕ (Ns g ⁻¹) ^f	/ _{sp} (Eq. 5) (Ns g⁻¹)
85/15 1f/AB°	85.02	0.0295	1.853	2.88	2.80 (-2.69%)
85/15 3u/AB°	60.58	0.0295	1.609	2.72	2.59 (-4.78%)
85/15 3v/AB°	76.92	0.0295	1.772	2.83	2.73 (-3.37%)
85/15 1e/AB	85.49	0.0304	1.889	2.86	2.85 (-0.49%)
				-(0)	

Chemical compositions: "(Wingborg et al. 2010); "(Manelis and Lempert 2009); "(Oyumi et al. 1996); "(Gadiot et al. 1993); "(Shastin and Lempert 2014); "Equilibrium specific impulses were calculated using the ISPBKW thermochemical code (Mader 2008). Heat of formation (HOF) values: AN (Dobratz and Crawford 1985); AB, PMVT and PVMDD (Manelis and Lempert 2009); TMETN (NIST 2017); HTPB (HOF) and atomic composition (Maggi and De Luca 2011); 3u and 3v (Shastin and Lempert 2014).

etc., all of which should work together in order to deliver the required thrust (Sutton and Biblarz 2001). Moreover, and in contrast to solid propellants, the fuel and the oxidizer that make up the liquid bipropellant are kept in separate tanks and are only mixed when injected into the engine's combustion chamber.

It is important to note, that an optimal mixing ratio (mass of oxidizer to mass of fuel, O/F) is carefully chosen not only to obtain high specific impulse, but also to keep the combustion temperature at an acceptable level.

The two major groups of bipropellant systems used today in (LRE) are cryogenic and storable propellants. The selection of one of these is influenced by many factors such as performance, cost, handling, toxicity, supply, and storage considerations. Other missile or space shuttle components like the auxiliary power drives and the roll-control thrusters (Huzel and Huang 1992)

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A Reliable Method for Predicting the Specific Impulse of Chemical Propellants

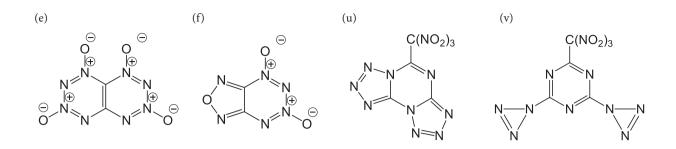


Figure 3. Structural formulas of C-N-O organic oxidizers used in composite propellants.

Table 8. Comparison between the specific impulse values calculated using the ISPBKW code and Eq. 5 for liquid monopropellant compositions. Percentage deviations in parentheses.

Liquid monopropellant compositions	Δ <i>H</i> ° _f (kcal mol⁻¹)	N _g	Ø∕(kcal g⁻¹)	/ _{<i>sp</i>} ∕ (Ns g⁻¹)º	/ _{sp} (Eq. 5) (Ns g⁻¹)
69.7/0.6/14.79/14.91 HAN/AN/MeOH/H ₂ O ^a	-141.34	0.0445	0.915	2.27	2.29 (1.14%)
77.25/0.67/17.19/4.89 HAN/AN/MeOH/H ₂ O ^a	-113.94	0.0433	1.085	2.43	2.43 (0%)
72.3/0.62/11.62/15.47 HAN/AN/EtOH/H ₂ O ^b	-135.98	0.0440	0.927	2.31	2.29 (-0.50%)
73.41/0.63/10.26/15.70 HAN/AN/ 1-PrOH/H ₂ O ^b	-133.49	0.0439	0.938	2.31	2.30 (-0.58%)
63.63/0.54/22.22/13.61 HAN/AN/Glycine/H $_2{\rm O}^{\rm b}$	-142.33	0.0425	0.771	2.15	2.08 (-3.08%)
60/30/10 ADN/MAN/Urea ^c	-57.54	0.0411	1.105	2.45	2.40 (-2.17%)
40/40/20 ADN/MAN/Urea ^c	-73.95	0.0415	0.902	2.20	2.20 (0)
30/40/30 ADN/MAN/Urea ^c	-84.31	0.0416	0.744	1.97	2.03 (2.68%)
59.86/25/15.14 $\rm H_2O_2(70\%)/AN/EtOH^d$	-172.85	0.0460	0.908	2.27	2.33 (2.56%)
80/8/12 H ₂ O ₂ (70%)/H ₂ O/EtOH ^d	-213.13	0.0477	0.828	2.19	2.29 (4.51%)
36.67/51.20/12.13 H ₂ O ₂ (70%)/ADN/EtOH ^d	-108.13	0.0434	1.137	2.47	2.48 (0.45%)

Chemical compositions: "(Chang et al. 2002); "(Wucherer et al. 2000); "(Ide et al. 2015); "(Martin et al. 2006); "Equilibrium specific impulses were calculated using the ISPBKW thermochemical code (Mader 2008). Heat of formation (HOF) values: HAN (Meng et al. 2009); MeOH, H₂O, EtOH, 1-PrOH, Glycine and Urea (NIST 2017); H₂O₂ (70%) (Constantine and Cain 1967).

employ monopropellant systems that, unlike bipropellants, do not require an external oxidizer source in order to undergo an exothermic reaction. Only monopropellants formed by an oxidizer and a fuel dissolved in a homogenous liquid phase will be treated here; however other classes of liquid monopropellants also exist. For example nitromethane and isopropyl nitrate are those monopropellants where both the oxidizer and the fuel are held together through covalent bonds in the same molecule. The final class of liquid monopropellants includes those materials formed by an unstable arrangement of atoms such as hydrogen peroxide and hydrazine which, when brought into contact with a suitable catalyst, will decompose with the generation of thermal energy and gaseous products (U.S. Army Material Command 1969). Some representative liquid monopropellant and bipropellant compositions, along with their calculated performance characteristics, are shown in Tables 8 and 9. As it is evident from the two tables and the percentage deviation values, the specific impulse estimated using Eq. 5 compare favorably with the output of ISPBKW thermochemical code.

HYBRID PROPELLANTS

The concept of a hybrid rocket, which employs a solid fuel and a liquid oxidizer (or vice-versa) as a propellant, is not new and dates back to the early 1930s (Krishnan 2002). In a typical hybrid rocket a highly pressurized gas is used to inject liquid



		J			
Liquid bipropellant compositions	∆ <i>H</i> ° _f (kcal mol⁻¹)	N _g	<i>Q∕</i> (kcal g⁻¹)	<i>I_{sp}∕</i> (Ns g⁻¹)⁰	/ _{sp} (Eq. 5) (Ns g⁻¹)
$N_2O_4/HEH (O/F = 1.94)^a$	-24.10	0.0372	1.511	2.68	2.68 (0)
N_2O_4 -UDMH/HEH (80/20) (O/F = 2.45) ^a	-2.58	0.0374	1.660	2.79	2.81 (0.92%)
N_2O_4 -UDMH/HEH (90/10) (O/F = 2.55) ^a	-0.42	0.0374	1.679	2.80	2.83 (1.06%)
$N_{2}O_{4}/UDMH (O/F = 2.60)^{a}$	2.05	0.0374	1.696	2.81	2.84 (1.17%)
N ₂ O ₄ -UDMH/HEH (60/40) (O/F= 2.32) ^a	-5.94	0.0374	1.641	2.77	2.79 (0.87%)
RFNA/UDMH $(O/F = 2.92)^{a}$	-43.83	0.0393	1.460	2.68	2.68 (0)
RFNA-UDMH/HEH (90/10) (O/F = 2.85) ^a	-45.77	0.0393	1.444	2.67	2.67 (0)
RFNA/HEH $(O/F = 2.14)^a$	-64.32	0.0390	1.304	2.57	2.53 (-1.43%)
$O_2/RP-1 (O/F = 2.60)^b$	-18.41	0.0323	2.146	2.94	3.09 (5.27%)
$O_2/N_2H_4 (O/F = 0.91)^b$	15.16	0.0476	1.905	3.07	3.21(4.62%)
$O_2/Toluene (O/F = 1.87)^{c}$	-5.19	0.0279	2.026	2.84	2.91 (2.58%)
O ₂ /Methylcyclohexane (O/F= 2.04) ^c	-21.69	0.0327	2.007	2.87	2.99 (4.29%)
O_2/n -heptane (O/F = 2.05) ^c	-24.03	0.0341	2.017	2.88	3.03 (5.09%)
O_2 /Ethylene oxide (O/F = 1.10) ^d	-29.72	0.0326	1.985	2.87	2.97 (3.72%)
O_2 /Nitroethane (O/ F= 0.65) ^d	-31.58	0.0345	1.818	2.81	2.88 (2.61%)
$O_2/EtOH-75\% (O/F = 1.30)^d$	-93.22	0.0379	1.640	2.71	2.80 (3.29%)
$TNM/N_2H_4 (O/F = 1.40)^d$	18.38	0.0438	1.586	2.85	2.89 (1.27%)
$H_2O_2 (90\%)/N_2H_4 (O/F = 1.50)^d$	-79.15	0.0522	1.335	2.70	2.86 (5.90%)
RFNA-DETA/MA (80/20) $(O/F = 3.00)^d$	-54.24	0.0388	1.364	2.61	2.58 (-0.94%)
RFNA/Hydine $(O/F = 3.17)^{b}$	-48.55	0.0387	1.433	2.65	2.64 (-0.36%)
$N_2O_4/N_2H_4 (O/F = 1.30)^{b}$	13.52	0.0456	1.584	2.87	2.92 (1.70%)
N_2O_4 /Aerozine-50 (O/F = 2.00) ^b	6.32	0.0405	1.658	2.83	2.87 (1.41%)
$N_2O_4/NO (70/30)$ -MeOH (O/F = 2.10) ^d	-45.03	0.0373	1.528	2.67	2.70 (0.90%)
$N_2O_4/NO (70/30)-NH_3 (O/F = 2.10)^d$	-20.17	0.0459	1.393	2.73	2.77 (1.38%)

Table 9. Comparison between the specific impulse values calculated using the ISPBKW code andEq. 5 for liquid bipropellant compositions. Percentage deviations in parentheses.

Chemical compositions: "(Keshavarz *et al.* 2011); ^b(U.S. Army Material Command 1969); "(Greenfield 1960); ^d(U.S. Army Ordnance Corps 1960); ^eEquilibrium specific impulses were calculated using the ISPBKW thermochemical code (Mader 2008). Heat of formation (HOF) values: N₂O₄, Toluene, Methylcyclohexane, n-heptane, Ethylene oxide, Nitroethane, N₂H₄, DETA, MA and TNM (NIST 2017); HEH and UDMH (Keshavarz *et al.* 2011); RFNA (Wright 1977); O₂, NO, RP-1, NH₃ (U.S. Army Material Command 1969).

oxidizer into the combustion chamber containing the solid grain fuel which causes the later to erode and vaporize leading to ignition and subsequent combustion. It is also well known that hybrid propellants burn as a macroscopic turbulent diffusion flame where the mixing ratio differs along the length of the grain, unlike solid and liquid propellants where the (O/F) value is uniform throughout the combustion chamber (Altman and Holzman 2007). Some features, like safety, the possibility to restart, and low cost are only few of the advantages that a hybrid rocket has over (SRM) and (LRE). A number of hybrid propellant formulations are shown in Table 10 along with their mixture ratios, from which the specific impulse was computed using the ISPBKW code and Eq. 5.

Many hybrid compositions typically employ HTPB as fuel due to its ease of processing, low cost of production and availability (Sutton and Biblarz 2001). The results of specific impulse calculations show that, as in the case of solid and liquid propellants, Eq. 5 is also valid to estimate the specific impulse of hybrid formulations and an expected deviation of $\pm 3 - 5\%$ from ISPBKW code is obtained for all tested samples.



 Table 10. Comparison between the specific impulse values calculated using the ISPBKW code and Eq. 5 for hybrid propellant compositions. Percentage deviations in parentheses.

Hybrid propellant compositions	∆ <i>H</i> ° _f (kcal mol⁻¹)	N _g	@∕(kcal g⁻¹)	<i>I_{sp}∕</i> (Ns g⁻¹)⁰	/ _{sp} (Eq. 5) (Ns g⁻¹)
$O_2/HTPB (O/F = 2.30)^a$	-10.91	0.0303	2.144	2.91	3.05 (4.82%)
H_2O_2 (90%)/PE (O/F = 7.80) ^a	-144.43	0.0442	1.385	2.63	2.73 (3.78%)
H_2O_2 (98%)/PE (O/F = 7.00) ^a	-125.53	0.0433	1.540	2.71	2.84 (4.56%)
H_2O_2 (98%)/DCPD (O/F = 6.20) ^a	-112.37	0.0413	1.600	2.70	2.84 (5.33%)
H_2O_2 (86%)/HTPB (O/F = 7.50) ^b	-117.89	0.0436	1.633	2.76	2.92 (5.60%)
$H_{2}O_{2} (92\%)/HTPB (O/F = 6.50)^{b}$	-116.24	0.0428	1.609	2.75	2.88 (4.89%)
RFNA/HTPB $(O/F = 4.90)^{\circ}$	-57.08	0.0344	1.457	2.54	2.56 (0.87%)
RFNA-HTPB/AP (90/10) (O/F = 3.80) ^c	-56.01	0.0343	1.427	2.56	2.54 (-1.09%)
$N_2O/Paraffin wax (O/F = 7.00)^d$	32.64	0.0344	1.359	2.60	2.47 (-4.77%)
$N_2O/HTPB (O/F = 7.40)^a$	37.38	0.0334	1.396	2.61	2.48 (-4.84%)
HAN(95%)/HTPB (O/F = 9.60) ^a	-89.89	0.0410	1.189	2.49	2.47 (-0.55%)

Chemical compositions: "(Heister and Wernimont 2007); "(Rajesh *et al.* 2003); "(Venugopal *et al.* 2011); "(Bernard *et al.* 2011); "Equilibrium specific impulses were calculated using the ISPBKW thermochemical code (Mader 2008). Heat of formation (HOF) values: DCPD (Shark *et al.* 2013); H₂D₂ (92%) and H₂D₂ (86%) (Rajesh *et al.* 2003); H₂D₄ (90%) and H₂D₂ (98%) (Constantine and Cain 1967); N₂D (Heister and Wernimont 2007); Paraffin wax (Bernard *et al.* 2011); PE (Risha *et al.* 2007).

CONCLUSION AND FUTURE SCOPE

The principal aim of the present study is to prove that, for a large body of C-H-N-O containing propellants, the specific impulse (I_{sp}) can be accurately obtained by applying Eq. 5 that employs only two variables, namely, the heat of reaction (*Q*) and the number of moles of gaseous reaction products per gram of propellant (N_g) calculated according to the well-known $[H_2O-CO_2]$ arbitrary decomposition assumption, which is a method proposed and used by chemist Mortimer J. Kamlet and physicist Sigmund J. Jacobs to predict condensed high explosives performance in the late 1960s. Throughout the present study, Eq. 5 was used to estimate the (I_{sp}) of solid, liquid and hybrid propellants. The results were compared to the output of the ISPBKW code, which shows that a deviation of no more than $\pm 3 - 4\%$ was obtained in most cases. Finally, future work should be directed toward finding a modified form of Eq. 5 capable of predicting the specific impulse of propellant formulations containing chlorine-based oxidizers and metals such as aluminum and boron.

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APPENDIX: GLOSSARY OF COMPOUND NAMES AND ATOMIC COMPOSITIONS

AB: Active binder, poly(methylvinyltetrazole)/NG/2,4-dinitro-2,4-diazapentane ($C_{10}H_{24,5}N_{10}O_{20,5}$) **ADN:** Ammonium dinitramide (H,N,O,) **Aerozine-50:** 50/50 hydrazine/UDMH (C₁₆₆₇H_{12,909}N_{4,788}) **AN:** Ammonium nitrate (NH₄NO₂) AP: Ammonium perchlorate (NH,ClO,) **BAMO:** 3,3-bis(azidomethyl)oxetane (C₄H₆N₆O)_n BDNPA-F: bis(2,2-dinitropropyl) acetal/bis(2,2-dinitropropyl) formal, 50/50 (C2,347H4,068N1,254O3,134) **BTNEU:** 1,3-bis(2,2,2-trinitroethyl)urea (C_cH_cN_oO₁₂) BTTN: 1,2,4-Butanetriol trinitrate (C₄H₂N₂O₂) Comp-B: 63/36/1 RDX/TNT /Wax (C203H264N218O267) **CL-20:** 2,4,6,8,10,12-Hexanitro-2,4,6,8,10,12-hexaazaisowurtzitane (C₄H₄N₁₂O₁₂) Cyclotol 60/40: RDX/TNT (C 204H2 50N2 15O2 68) **DCPD:** Dicyclopentadiene $(C_{10}H_{12})$ **DEGDN:** Diethyleneglycol Dinitrate ($C_4H_0N_2O_7$) **DEP:** Diethyl Phthalate $(C_{12}H_{14}O_4)$ **DETA:** Diethylenetriamine (C₄H₁₂N₂) **DDNP:** Diazodinitrophenol $(C_{\epsilon}H_{\gamma}N_{4}O_{\epsilon})$ **DINA:** Dioxyethylnitramine Dinitrate (C₄H₂N₄O₂) DIPAM: 3,3'-diamino-2,2',4,4',6,6'-hexanitrobiphenyl (C₁₂H_eN_oO₁₂) **DIPEHN:** Dipentaerythritol Hexanitrate $(C_{10}H_{14}N_{e}O_{10})$ **DNDMOxm:** Dinitrodimethyloxamide (C₄H₆N₄O₆) **DNOC:** 4,6-Dinitro-*o*-cresol $(C_{\tau}H_{\epsilon}N_{\gamma}O_{\epsilon})$ **DNPH:** (2,4-Dinitrophenyl)hydrazine ($C_e H_e N_A O_A$) **EDDN:** Ethylenediamine Dinitrate $(C_2H_{10}N_2O_2)$ **EDNA:** Ethylenedinitramine $(C_2H_6N_4O_4)$ **ETN:** Ethriol Trinitrate $(C_6H_{11}N_3O_9)$ FOX-7: 1,1-Diamino-2,2-dinitroethene (C₂H₄N₄O₄) FOX-12: N-guanylurea-dinitramide (C₂H₂N₂O₂) **GAP:** Glycidyl azide polymer $(C_2H_2N_2O)_{12}$ GUNI: Guanidine Nitrate (CH, N, O,) **HAN:** Hydroxylammonium nitrate $(H_4N_5O_4)$ **HEH:** Hydroxyethylhydrazine (C₂H₂N₂O) HMX: 1,3,5,7-Tetranitro-1,3,5,7-tetraazacyclooctane (C₄H₈N₈O₈) HNAB: 2,2,4,4,6,6'-Hexanitroazobenzene (C₁₂H₄N₈O₁₂) HNF: Hydrazinium nitroformate (CH₅N₅O₆) HNS: 2,2,4,4,6,6'-Hexanitrostilbene (C, H, N, O,) HTPB: Hydroxyl-terminated polybutadiene (C_{7.075}H_{10.65}N_{0.063}O_{0.223}) Hydine: 60/40 UDMH/DETA (C_{3.551}H_{13.040}N_{3.163}) LX-14: 95/5 HMX/Estane (C152H292N259O266) MA: Methylamine (CH₂N) NG: Nitroglycerine (C₃H₅N₃O₉) **NQ:** Nitroguanidine $(CH_4N_4O_2)$ NM: Nitromethane (CH₃NO₂)



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Octol 75/25: 75/25 HMX/TNT (C_{1 78}H_{2.58}N_{2.36}0_{2.69}) **PA:** Picric Acid (C₆H₃N₃O₇) Paraffin wax: $(C_{50}H_{102})$ **PBX-9007:** 90/9.1/0.5/0.4 RDX/PS/DOP/Rosin (C₁₉₇H₃₂₂N₂₄₃O₂₄₄) **PBX-9011:** 90/10 HMX/Estane (C_{1.73}H_{3.18}N_{2.45}O_{2.61}) **PBX-9404:** 94/3/3 HMX/Nitrocellulose/ Tris- β -Chloroethyl phosphate (C_{1,40}H_{2,75}N_{2,57}O_{2,69}Cl_{0.03}P_{0.01}) **PBX-9501:** 95/2.5/2.25 HMX/Estane/BDNPF (C_{1.47}H_{2.86}N_{2.60}O_{2.69}) **PE:** Polyethylene $(C_2H_4)_n$ **Pentolite (50/50):** 50/50 TNT/PETN (C_{2,33}H_{2,37}N_{1,29}O_{3,22}) **PETN:** Pentaerythritol tetranitrate ($C_{e}H_{o}N_{d}O_{12}$) **PGN:** poly(glycidyl nitrate) (C₁H₂N₁O₄) **PLN:** Polynitromethyloxetane $(C_2H_0N_1O_4)_n$ **PMVT:** Poly(methylvinyltetrazole) $(C_4H_4N_4)_{n}$ **PVMDO:** Poly(vinylmethoxydiazen-N-oxide) (C₃H₆N₂O₂)₁ RDX: 1,3,5-Trinitro-1,3,5-triazacyclohexane (C,H,N,O,) **RFNA:** Red fuming nitric acid 84/14/2 HNO₃/NO₂/H₂O (H_{0.931}N_{0.981}O_{2.826}) **RP-1:** Mixture of naphthenes/paraffins/ C_{12} olefins (CH_{1.95})_n **TAGAZ:** Triaminoguanidinium azotetrazolate ($C_4H_0N_{22}$) **TATB:** 1,3,5-Triamino-2,4,6-trinitrobenzene (C₆H₆N₆O₆) **Tetryl:** 2,4,6-Trinitrophenyl-N-methylnitramine (C₇H₅N₅O₈) **TMETN:** Trimethylolethane trinitrate ($C_{E}H_{0}N_{2}O_{0}$) **TNM:** Tetranitromethane (CN₄O₆) TNT: 2,4,6-Trinitrotoluene (C₇H₅N₃O₆) NC (12%N): Nitrocellulose $(C_{4}H_{7,74}N_{3,76}O_{0,57})$ NC (13.35%N): Nitrocellulose (C₆H_{7.29}N_{2.71}O_{10.41}) **UDMH:** Unsymmetrical dimethylhydrazine (C₂H₂N₂) 2-NDPA: 2-Nitrodiphenylamine (C₁₂H₁₀N₂O₂) 1a: 2,4,6,2,4,6'-Hexanitrodiphenylamine $(C_{12}H_{\epsilon}N_{7}O_{12})$ **1b**: Mannitol Hexanitrate (C₆H₈N₆O₁₈) 1c: MAN, Methylamine Nitrate (CH₂N₂O₂) 1d: BTF, Benzotris[1,2,5]oxadiazole-1,4,7-trioxide (C₄N₆O₄) 1e: DTTO, di-1,2,3,4-tetrazine tetraoxide ($C_2N_8O_4$) 1f: FTDO, [1,2,5]Oxadiazolo[3,4-e][1,2,3,4]-Tetrazine-4,6- di-N-Oxide (C₂N₆O₃) 1g: TKX-50, dihydroxylammonium 5,5'-bistetrazole-1,1'-diolate (C₂H₂N₁₀O₄) **1h**: ANTX, Ammonium 5-Nitrotetrazolate-2*N*-oxide (CH₄N₆O₃) 1i: 5-Nitrotetrazole-2N-oxide (CHN₂O₂) 1j: HxNTX, Hydroxylammonium 5-Nitrotetrazolate-2N-oxide (CH₄N₆O₄) 1k: GNTX, Guanidinium 5-Nitrotetrazolate-2N-oxide (C₂H₂N₂O₂) 11: AGNTX, Aminoguanidinium 5-Nitrotetrazolate-2N-oxide (C₂H₂N₉O₃) 1m: TAGNTX, Triaminoguanidinium 5-Nitrotetrazolate-2N-oxide (C₂H₀N₁₁O₂) 1n: 5-Aminohydroximoyl-2-hydroxytetrazole (C₂H₄N₆O₂) 10: Hydroxylammonium 5-aminohydroxyimoyl-tetrazole-2-oxide (C₂H₂N₂O₂) 1p: 1,2,3,4,5-pentanitrobicyclo[1.1.1]pentane (C₅H₃N₅O₁₀) 1q: Nitryl cyanide (CN₂O₂) **1r**: Hexaazabenzene (N₆)

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1s: Octaazacubane (N_a)

1t: Bipentazole (N₁₀)

3u: 5-Trinitromethyl-bistetrazolo[1,5-a:1,5'-c][1,3,5]triazine ($C_4N_{12}O_6$)

3v: Di(1H-triazirin-1-yl)-6-trinitromethyl-1,3,5-triazine ($C_4N_{12}O_6$)

M1: 83.13/9.78/4.89/0.98/0.73/0.49 NC (13.15%N)/Dinitrotoluene/Dibutylphthalate/Diphenylamine/Ethyl alcohol/Water (C2535H3102N0884O3370) M1A1: 83.17/9.84/4.44/0.98/0.98/0.59 NC (12.60%N)/Dinitrotoluene/Dibutylphthalate/Diphenylamine/Ethyl alcohol/Water (C2 577 H3 737 H3 7 M6: 84.96/9.77/2.93/0.98/0.88/0.49 NC (13.15%N)/Dinitrotoluene/Dibutylphthalate/Diphenylamine/Ethyl alcohol/Water (C2467H3015N09100341) M10: 96.93/0.99/0.10/1.48/0.49 NC (13.15%N)/Diphenylamine/Graphite/ Ethyl alcohol/Water (C2214H2854N0916O3666) M12: 89.63/7.34/0.73/1.38/0.98 NC (13.15%N)/Dinitrotoluene/Diphenylamine/Ethyl alcohol/Water (C, 100H, 2070, 507) M14: 88.02/7.82/1.96/0.98/0.98/0.25 NC (13.15%N)/Dinitrotoluene/Dibutylphthalate Diphenylamine/Ethyl alcohol/Water (C2, 200 H2, 240 N0, 918 O3, 45%) IMR: 89.92/7.19/0.63/1.35/0.90 NC (13.15%N)/Dinitrotoluene/Diphenylamine/Ethyl alcohol/Water (C2.301 H2.912 N0.927 O3.527) M2: 76.80/19.34/0.59/0.30/2.28/0.69 NC (13.25%N)/NG/Ethyl centralite/Graphite/Ethyl alcohol/Water (C_{2.049}H_{2.837}N_{0.986}O_{3.669}) M5: 81.26/14.87/0.59/0.30/2.28/0.69 NC (13.25%N)/NG/Ethyl centralite/Graphite/Ethyl alcohol/Water (C_{2, 052}H_{2, 052}O_{2, 652}) M7: 58.71/38.17/0.97/0.86/1.29 NC (13.15%N)/NG/Ethyl centralite/ Ethyl alcohol/Carbon black (C1965H2 565N1065O3 683) M8: 52.60/43.47/0.61/0.40/3.03 NC (13.25%N)/NG/Ethyl centralite/ Ethyl alcohol/Diethylphthalate (C_{1.911}H_{2.609}N_{1.075}O_{3.710}) M9: 58.33/40.40/0.76/0.51 NC (13.25%N)/NG/Ethyl centralite/ Ethyl alcohol (C_{1.844}H_{2.527}N_{1.091}O_{3.751}) $\textbf{M18:} 79.60/9.95/8.96/1.00/0.50 \text{ NC } (13.15\%)/\text{NG/Dibutylphthalate/Diphenylamine/Ethyl alcohol } (C_{2.440}\text{H}_{3.145}\text{N}_{0.885}\text{O}_{3.446})/(C_{2.440}\text{H}_{3.45}\text{N}_{0.86}\text{O}_{3.46})/(C_{2.440}\text{H}_{3.45}\text{O$ **M26**: 67.22/24.99/6.00/0.30/1.20/0.30 NC (13.15%N)/NG/Ethyl centralite/Graphite/Ethyl alcohol/ Water (C_{3.20}H_{3.05}N_{1.06}O_{3.51}E) T25: 73.21/19.99/5.00/0.30/1.20/0.30 NC (13.15%N)/NG/Ethyl centralite/Graphite/Ethyl alcohol/ Water (C, 2022H, 2010 C (13.15\%N)/NG/Ethyl centralite/Graphite/Ethyl alcohol/ Water (C, 2010 C (13.15\%N)/NG/Ethyl alcohol/ Water (C, 2010 C (13.15\%N)/NG/Ethyl alcohol/ Water (C, 2010 C (13.15\%N)/NG/Ethyl alcohol/ Water (C, 2010 C (13.15 M15: 20.00/19.00/54.70/6.00/0.30 NC (13.15%N)/NG/NQ/Ethyl centralite/Ethyl alcohol (C_{1.50}/H_{3.530}N_{3.566}O_{3.566}) M17: 21.98/21.48/54.65/1.50/0.10/0.30/0.10 NC (13.15%N)/NG/NQ/Ethyl centralite/ Graphite/Ethyl alcohol/Water (C_{1,387}H_{3,301}N_{2,602}O_{2,718}) **T34**: 20.00/19.00/54.70/4.00/2.00/0.30 NC (12.60%N)/NG/NQ/Dibutylphthalate/2-Nitrodiphenylamine/Ethyl alcohol (C_{1.572}H_{3.574}N_{2.552}O_{2.614}) 28/22.5/1.5/48 NC(12%N)/NG/Carbamite/Picrite: C1400H3 273N2 393O2 830 28/22.5/1.5/48 NC(13.35%N)/NG/Carbamite/Picrite: C1445H3171N2420O2846 20.8/20.6/3.6/55 NC(13.35%N)/NG/Carbamite/Picrite: C1.468H3.369N2.645 28/22.5/1.5/38/10 NC(12%N)/NG/Carbamite/Picrite/RDX: C_{1.529}H_{3.159}N_{2.278}O_{2.908} 28/22.5/1.5/33/15 NC(12%N)/NG/Carbamite/Picrite/RDX: C1548H3102N222IO2947 28/22.5/1.5/28/20 NC(12%N)/NG/Carbamite/Picrite/RDX: C_{1.568}H_{3.045}N_{2.164}O_{2.986} 29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/AP: C_{1.598}H_{3.150}N_{0.944}O_{3.469}Cl_{0.251} 29.5/32/2/1/29.5/6 DNC/NG/DEP/2-NDPA/AP/BDNPA-F: C₁₄₁₅H₃₀₁₆N₁₀₂₀O₃₅₄₉Cl₀₂₅₁ 29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/RDX: C_{1.996}H_{2.942}N_{1.490}O_{3.261} 29.5/32/2/1/29.5/6 DNC/NG/DEP/2-NDPA/RDX/BDNPA-F: C₁₈₁₃H_{2.808}N_{1.565}O_{3.341} **29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/ADN:** C₁₅₉₈H_{3.096}N_{1.644}O_{3.416} 29.5/32/8/1/29.5 DNC/NG/DEP/2-NDPA/HNF: C1 750H2 051N1 400O2 431 **30/40/30 DNC/CL/TAGAZ:** C_{1.908}H_{3.576}N_{2.448}O_{2.448}O 80/20 RDX/GAP: C_{1.687}H_{3.171}N_{2.767}O_{2.363} 71/9/20 RDX/GAP/BTTN: C_{1.564}H_{2.953}N_{2.440}O_{2.755} 70/30 HMX/GAP: C1854H3406N28002194 **80/20 RDX/BAMO:** C_{1.600}H_{2.940}N_{2.940}O_{2.291} 70/30 HMX/BAMO: C_{1.725}H_{3.059}N_{3.059}O_{2.085} 70/30 CL-20/GAP: C_{1.868}H_{2.474}N_{2.826}O_{2.220} 80/20 CL-20/BAMO: C1615 H1875 N2970 O2321 80/20 ADN/GAP: C_{0.606}H_{3.589}N_{3.185}O_{2.781} 75/25 ADN/GAP: C_{0.758}H_{3.681}N_{3.176}O_{2.671} **70/30 ADN/GAP:** C_{0.909}H_{3.772}N_{3.166}O_{2.560}

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65/35 ADN/GAP: C1061 H3863 N3156 O2449
60/40 ADN/GAP: C<sub>1.212</sub>H<sub>3.955</sub>N<sub>3.147</sub>O<sub>2.339</sub>
50/50 ADN/GAP: C<sub>1,515</sub>H<sub>4,137</sub>N<sub>3,127</sub>O<sub>2,117</sub>
74/26 ADN/AB: C<sub>0.494</sub>H<sub>3.282</sub>N<sub>2.880</sub>O<sub>3.153</sub>
85/15 ADN/PMVT: C<sub>0.545</sub>H<sub>3.559</sub>N<sub>3.286</sub>O<sub>2.741</sub>
80/20 ADN/PVMDO: C<sub>0.588</sub>H<sub>3.756</sub>N<sub>2.972</sub>O<sub>2.972</sub>O
75/25 AN/AB: C0475H4610N2349O3548
85/15 AN/PMVT: C<sub>0.545</sub>H<sub>5.066</sub>N<sub>2.669</sub>O<sub>3.186</sub>
85/15 AN/PVMDO: C<sub>0.441</sub>H<sub>5.130</sub>N<sub>2.418</sub>O<sub>3.480</sub>
60/20/20 AN/GAP/TMETN: C<sub>0.998</sub>H<sub>4.714</sub>N<sub>2.340</sub>O<sub>3.156</sub>
70/15/15 AN/GAP/TMETN: C_{0.749}H_{4.785}N_{2.380}O_{3.304}
60/15/15/10 AN/GAP/TMETN/NC(12%N): C<sub>0.976</sub>H<sub>4.578</sub>N<sub>2.216</sub>O<sub>3.290</sub>
40/15/15/30 AN/GAP/TMETN/NC(12%N): C1431H4165N1887O3262
40/15/15/30 AN/GAP/TMETN/HMX: C<sub>1.154</sub>H<sub>4.096</sub>N<sub>2.441</sub>O<sub>2.990</sub>
80/20 HNF/GAP: C1043H3195N2791O2824
80/20 HNF/PGN: C<sub>0.941</sub>H<sub>3.025</sub>N<sub>2.353</sub>O<sub>3.294</sub>
80/20 HNF/PLN: C<sub>0.925</sub>H<sub>3.648</sub>N<sub>2.347</sub>O<sub>3.272</sub>
80/20 HNF/BAMO: C<sub>0.956</sub>H<sub>2.964</sub>N<sub>2.964</sub>O<sub>2.752</sub>
80/20 HNF/HTPB: C<sub>1.852</sub>H<sub>4.315</sub>N<sub>2.197</sub>O<sub>2.666</sub>
85/15 1f/AB: C<sub>1.374</sub>H<sub>0.520</sub>N<sub>3.557</sub>O<sub>2.074</sub>
85/15 3u/AB: C<sub>1374</sub>H<sub>0520</sub>N<sub>3557</sub>O<sub>2074</sub>
85/15 3v/AB: C<sub>1374</sub>H<sub>0520</sub>N<sub>3557</sub>O<sub>2074</sub>
85/15 1e/AB: C<sub>1134</sub>H<sub>0520</sub>N<sub>3687</sub>O<sub>2140</sub>
69.70/0.6/14.79/14.91 HAN/AN/MeOH/H<sub>2</sub>O: C<sub>0.462</sub>H<sub>6.435</sub>N<sub>1.466</sub>O<sub>4.215</sub>
77.25/0.67/17.19/4.89 HAN/AN/MeOH/H<sub>2</sub>O: C<sub>0.537</sub>H<sub>5.940</sub>N<sub>1.625</sub>O<sub>4.051</sub>
72.30/0.62/11.62/15.47 HAN/AN/EtOH/H<sub>2</sub>O: C<sub>0.505</sub>H<sub>6.274</sub>N<sub>1.521</sub>O<sub>4.146</sub>
73.41/0.63/10.26/15.70 HAN/AN/1-PrOH/H<sub>2</sub>O: C<sub>0.512</sub>H<sub>6.198</sub>N<sub>1.544</sub>O<sub>4.124</sub>
63.63/0.54/22.22/13.61 HAN/AN/Glycine/H<sub>2</sub>O: C<sub>0.592</sub>H<sub>5.669</sub>N<sub>1.635</sub>O<sub>4.018</sub>
60/30/10 ADN/MAN/Urea: C<sub>0.485</sub>H<sub>4.514</sub>N<sub>2.905</sub>O<sub>3.058</sub>
40/40/20 ADN/MAN/Urea: C<sub>0.758</sub>H<sub>5.172</sub>N<sub>2.806</sub>O<sub>2.806</sub>O
30/40/30 ADN/MAN/Urea: C<sub>0.925</sub>H<sub>5.516</sub>N<sub>2.817</sub>O<sub>2.742</sub>
59.86/25/15.14 H<sub>2</sub>O<sub>2</sub>(70%)/AN/EtOH: C<sub>0.657</sub>H<sub>7.680</sub>N<sub>0.625</sub>O<sub>4.727</sub>
80/8/12 H,O,(70%)/H,O/EtOH: C<sub>0.521</sub>H<sub>8.410</sub>O<sub>5.330</sub>
36.67/51.20/12.13 H<sub>2</sub>O<sub>2</sub>(70%)/ADN/EtOH: C<sub>0.527</sub>H<sub>5.962</sub>N<sub>1.651</sub>O<sub>4.034</sub>
N_2O_4/HEH (O/F= 1.94): C_{0.895}H_{3.579}N_{2.330}O_{3.317}
N_{0_4}-UDMH/HEH (80/20) (O/F= 2.45): C_{0.927}H_{3.713}N_{2.471}O_{3.161}
N,O<sub>4</sub>-UDMH/HEH (90/10) (O/F= 2.55): C<sub>0.922</sub>H<sub>3.695</sub>N<sub>2.482</sub>O<sub>3.156</sub>
N_2O_4/UDMH (O/F=2.60): C_{0.927}H_{3.707}N_{2.496}O_{3.139}
N_{,O_{4}}-UDMH/HEH (60/40) (O/F= 2.32): C_{0.920}H_{3.679}N_{2.439}O_{3.196}
RFNA/UDMH (O/F=2.92): C<sub>0.850</sub>H<sub>4.559</sub>N<sub>2.070</sub>O<sub>3.516</sub>
RFNA-UDMH/HEH (90/10) (O/F= 2.85): C<sub>0.850</sub>H<sub>4.557</sub>N<sub>2.061</sub>O<sub>3.523</sub>
RFNA/HEH (O/F= 2.14): C<sub>0.837</sub>H<sub>4.408</sub>N<sub>1.954</sub>O<sub>3.637</sub>
O_2/RP-1 (O/F= 2.60): C_{1.989}H_{3.878}O_{4.513}
O_{2}/N_{2}H_{4} (O/F= 0.91): H_{6.529}N_{3.265}O_{2.981}
O<sub>1</sub>/Toluene (O/F= 1.87): C<sub>2.644</sub>H<sub>3.021</sub>O<sub>4.075</sub>
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 $O_{2,345}H_{4,691}O_{4,194}$ O_{2}/n -heptane (O/F= 2.05): $C_{2.291}H_{5.238}O_{4.200}$ O_{7} /Ethylene oxide (O/F= 1.10): $C_{2,157}H_{4,313}O_{4,360}$ O_2 /Nitroethane (O/F= 0.65): $C_{1.615}H_{4.037}N_{0.807}O_{4.077}$ O₂/EtOH-75% (O/F= 1.30): C₁₄₁₃H₅₄₄₅O₄₈₄₇ TNM/N₂H₄ (O/F= 1.40): $C_{0.298}H_{5.181}N_{3.784}O_{2.388}$ $H_{2,0}$, (90%)/N, H_{4} (O/F= 1.50): $H_{8,836}N_{2,497}O_{3,509}$ **RFNA-DETA/MA (80/20) (O/F= 3.00):** $C_{0.936}H_{4.491}N_{1.971}O_{3.539}$ **RFNA/Hydine (O/F= 3.17):** C_{0.852}H_{4.312}N_{2.004}O_{3.587} $N_{2}O_{4}/N_{2}H_{4}$ (O/F= 1.30): $H_{5.418}N_{3.940}O_{2.461}$ N_2O_4 /Aerozine-50 (O/F= 2.00): $C_{0.555}H_{4.299}N_{3.044}O_{2.900}$ N_2O_4/NO (70/30)-MeOH (O/F= 2.10): $C_{1.005}H_{4.020}N_{1.710}O_{3.746}$ $N_{2}O_{4}/NO$ (70/30)- NH_{3} (O/F= 2.10): $H_{5.672}N_{3.601}O_{2.741}$ **O₂/HTPB (O/F=2.30):** C_{2.144}H_{3.227}N_{0.019}O_{4.424} H,O, (90%)/PE (O/F=7.80): C_{0.814}H_{7.302}O_{5.181} **H**,**O**, (98%)/PE (O/F=7.00): C_{0.893}H_{7.023}O_{5.140} H₂O₂ (98%)/DCPD (O/F=6.20): C_{1.051}H_{6.415}O_{5.058} H₂O₂ (86%)/HTPB (O/F= 7.50): $C_{0.842}H_{7.093}N_{0.007}O_{5.167}$ H,O, (92%)/HTPB (O/F= 6.50): C_{0.941}H_{6.877}N_{0.008}O_{5.105} **RFNA/HTPB (O/F=4.90):** C_{1,196}H_{3,092}N_{1,371}O_{3,959} **RFNA-HTPB/AP (90/10) (O/F=3.80):** C_{1.324}H_{3.296}N_{1.326}O_{3.850}Cl_{0.018} N,O/Paraffin wax (O/F= 7.00): $C_{0.890}H_{1.816}N_{3.976}O_{1.988}$ $N_2O/HTPB$ (O/F= 7.40): $C_{0.842}H_{1.267}N_{4.011}O_{2.028}$ HAN(95%)/HTPB (O/F= 9.60): C_{0.665}H_{5.089}N_{1.798}O_{3.857}